

Solve each system. Check your answers:

①

$$\begin{cases} -3 \times \{ 2x + 4y = 10 \\ 2 \times \{ 3x + 5y = 11 \end{cases}$$

$$\begin{array}{r} -6x - 12y = -30 \\ + \quad 6x + 10y = 22 \\ \hline -2y = -8 \\ \frac{-2y}{-2} = \frac{-8}{-2} \end{array}$$

$$y = 4$$

$$2x + 4(4) = 10$$

$$\begin{array}{r} 2x + 16 = 10 \\ -16 \quad -16 \\ \hline 2x = -6 \end{array}$$

$$2x = -6$$

$$x = -3$$

②

$$\begin{cases} 4x + 2y = -4 \\ -8x - 4y = 8 \end{cases} \quad \begin{array}{l} \times 2 \Rightarrow 8x + 4y = -8 \\ \Rightarrow -8x - 4y = 8 \\ \hline \end{array}$$

$$\rightarrow 0 = 0$$

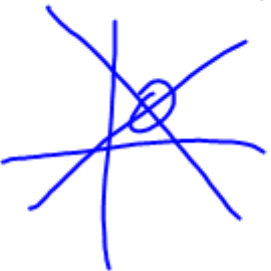
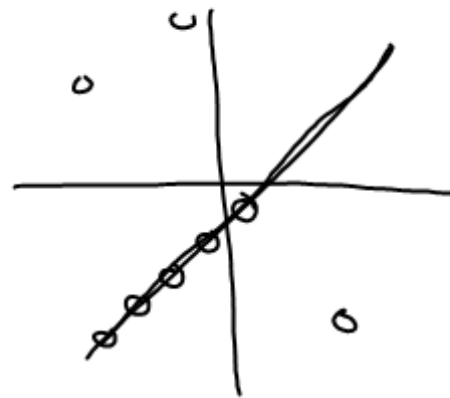
\rightarrow dependent

\rightarrow no unique solution

$$\rightarrow 4 = 0$$

\rightarrow no solution

\rightarrow inconsistent



$$2x + 4y = -2 \quad \times 2 \Rightarrow 4x + 8y = -4$$

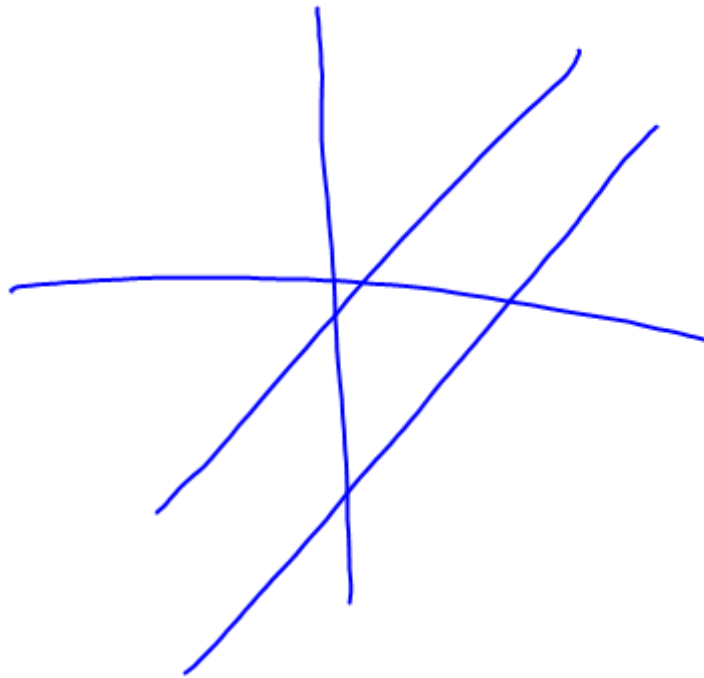
$$4x + 8y = 0$$

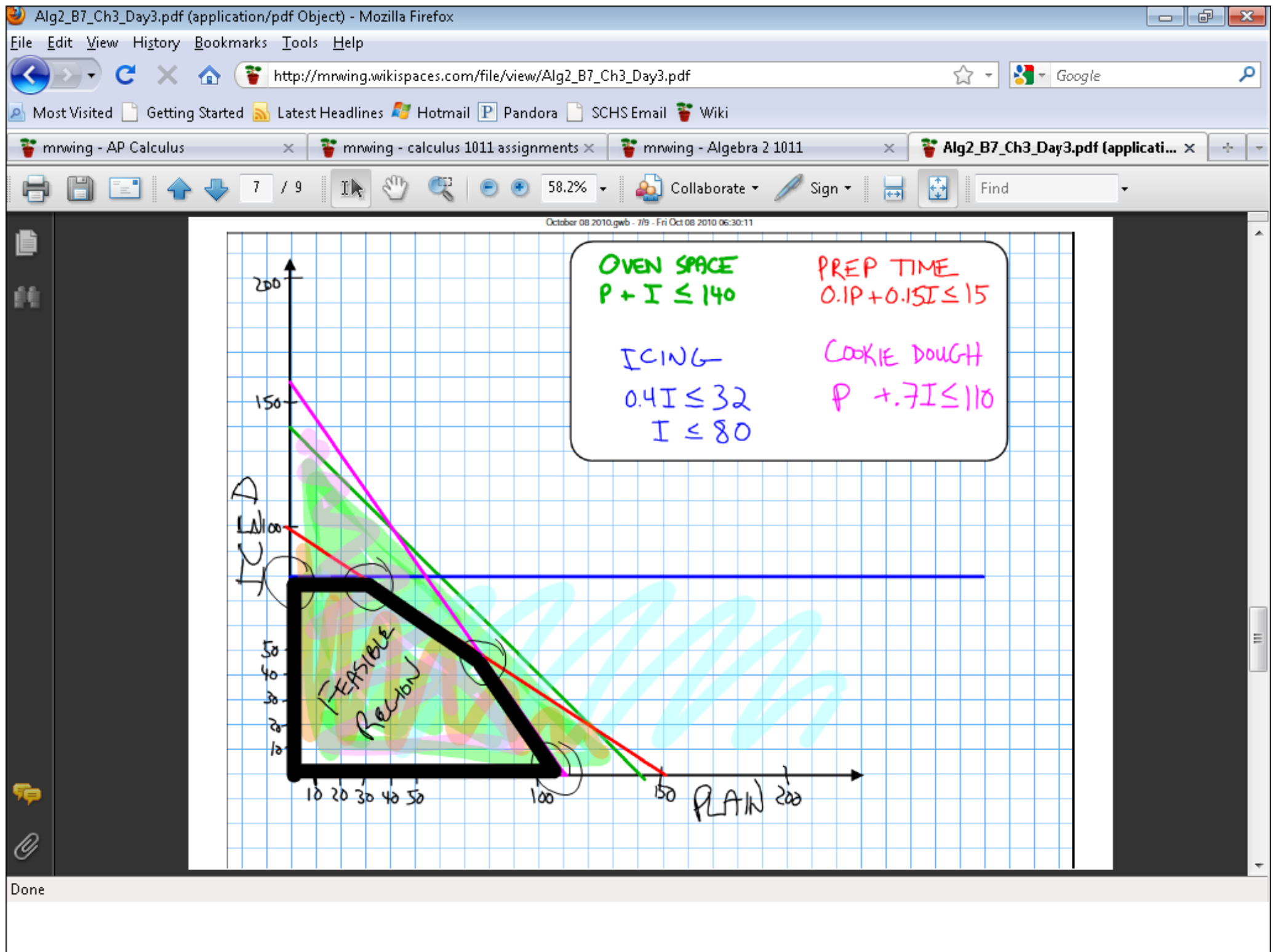
$$\Rightarrow (4x + 8y = 0)$$


$$\rightarrow 0 = -4$$

\rightarrow inconsistent

\rightarrow no solution





$$\begin{aligned} 1a) \quad y &= -3x + 4 \\ y &= 7x - 26 \end{aligned}$$

$$y = -3x + 4$$

$$\begin{array}{r} 7x - 26 = -3x + 4 \\ +3x \quad +26 \quad +3x \quad +26 \end{array}$$

$$10x = 30$$

$$x = 3$$

$$y = -3(3) + 4$$

$$y = -9 + 4$$

$$y = -5$$

$$\begin{aligned} b) \quad y &= 6x + 2 \\ 3x - 4y &= -29 \end{aligned}$$

$$1) \quad \begin{matrix} 3x & x + 7y = 12 \\ & 3x - 5y = 10 \end{matrix} \rightarrow \text{sub} \quad x = 12 - 7y$$

$$\begin{array}{r} -3x - 21y = -36 \\ + \quad 3x - 5y = 10 \\ \hline \end{array}$$

$$-26y = -26$$

$$y = 1$$

$$x + 7(1) = 12$$

$$x + 7 = 12$$

$$x = 5$$

2a)

$$x + y \geq 6$$

$$\frac{x-\text{int}}{6}$$

$$\frac{y-\text{int}}{6}$$

$$x \leq 8$$

$$8$$

$$y \leq 5$$

$$5$$

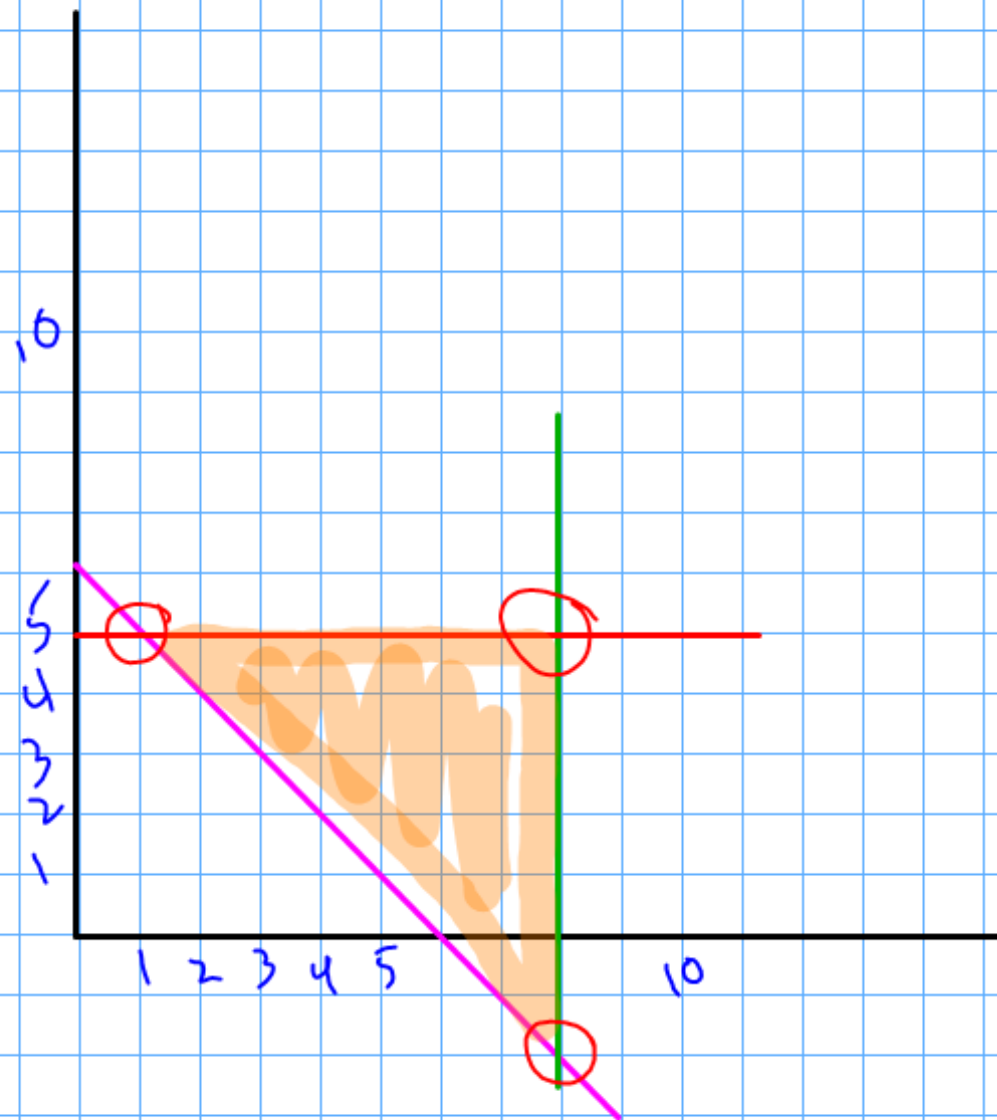
Minimize for
 $C = x + 3y$

$$(1, 5) \Rightarrow 1 + 3(5) = 16$$

$$(8, 5) \Rightarrow 8 + 3(5) = 23$$

$$(8, -2) \Rightarrow 8 + 3(-2) = 2$$

$$x = 8, y = -2$$



$$2b) \begin{cases} 3x + y \leq 7 \\ x + 2y \leq 9 \end{cases}$$

$$\begin{array}{cc} x\text{-int} & y\text{-int} \\ \frac{7}{3} = 2\frac{1}{3} & 7 \\ 9 & \frac{9}{2} = 4\frac{1}{2} \end{array}$$

$$x \geq 0$$

$$y \geq 0$$

$$(1, 4) \Rightarrow 2(1) + 4 = 6$$

Maximize for $(0, 5) \Rightarrow 0 + 5 = 5$

$$P = 2x + y \quad (2\frac{1}{3}, 0)$$

$$3x + y = 7$$

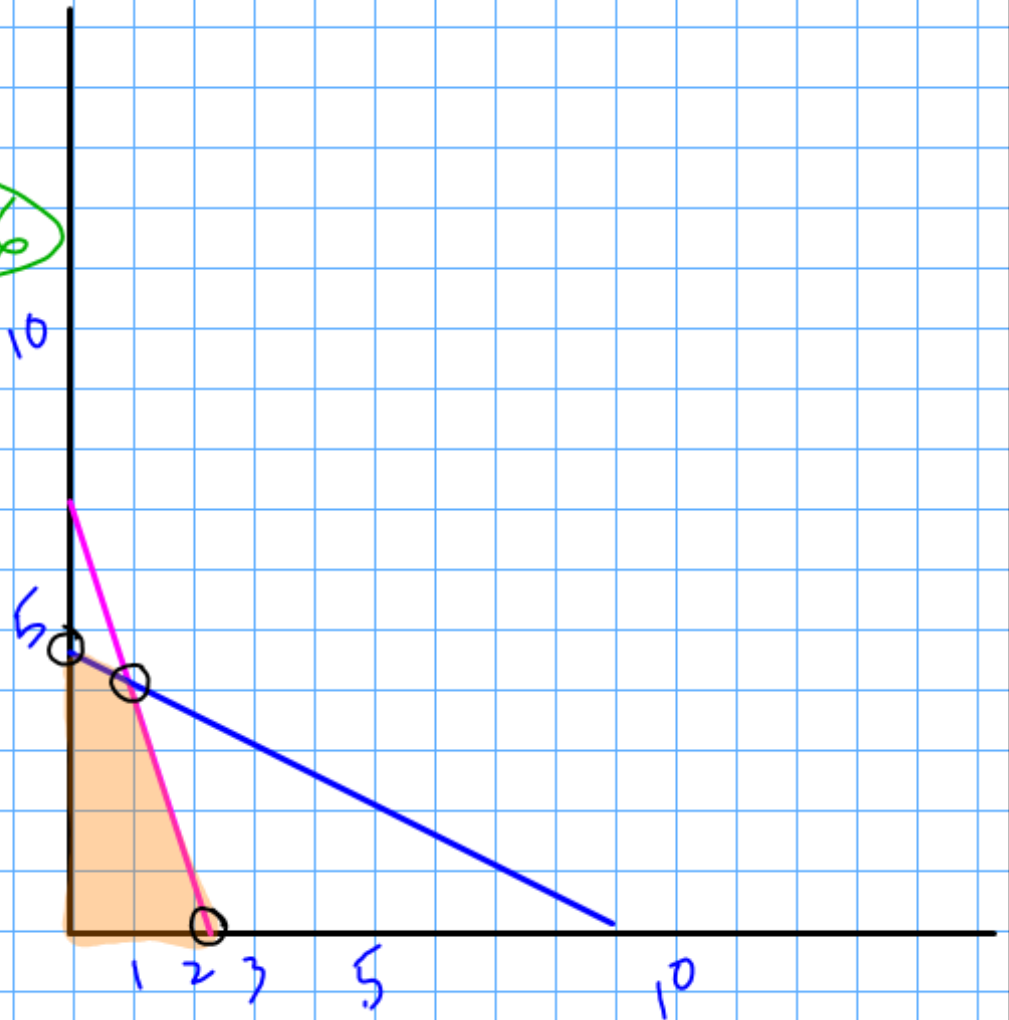
$$-3x(x + 2y = 9)$$

$$-3x - 6y = -27$$

$$3x + y = 7$$

$$-5y = -20$$

$$y = 4$$



3) Gonza Manufacturing has two factories that produce three grades of paper: low grade, medium grade, and high grade. It needs to supply at least 24 tons of low grade, 6 tons of medium grade, and 30 tons of high grade paper. Factory A produces 8 tons of low grade, 1 ton of medium grade, 2 tons of high grade paper daily, and costs \$2,000 per day to operate. Factory B produces 2 tons of low grade, 1 ton of medium grade, 8 tons of high grade paper daily, and costs \$4,000 per day to operate.

- Write the information above as inequalities using x for factory A and y for factory B.
- Graph the inequalities and make a clear sketch of the feasible region. Label all relevant points on your graph.
- How many days should each factory operate to fill the orders at minimum cost? What is the cost to fill the orders?

$x = \text{factory A}; y = \text{factory B}$

$$\begin{array}{ll} \text{Low} : & 8x + 2y \geq 24 \\ \text{Med} : & x + y \geq 6 \\ \text{High} : & 2x + 8y \geq 30 \end{array}$$

$$\text{minimum cost} = 2000x + 4000y$$

$$\begin{array}{rcl}
 8x + 2y \geq 24 & / & \begin{array}{l} \text{x-int } 3 \\ \text{y-int } 12 \end{array} \\
 x + y \geq 6 & / & \begin{array}{l} 6 \\ 6 \end{array} \\
 2x + 8y \geq 50 & / & \begin{array}{l} 15 \\ \frac{30}{8} = 3\frac{3}{4} \end{array}
 \end{array}$$

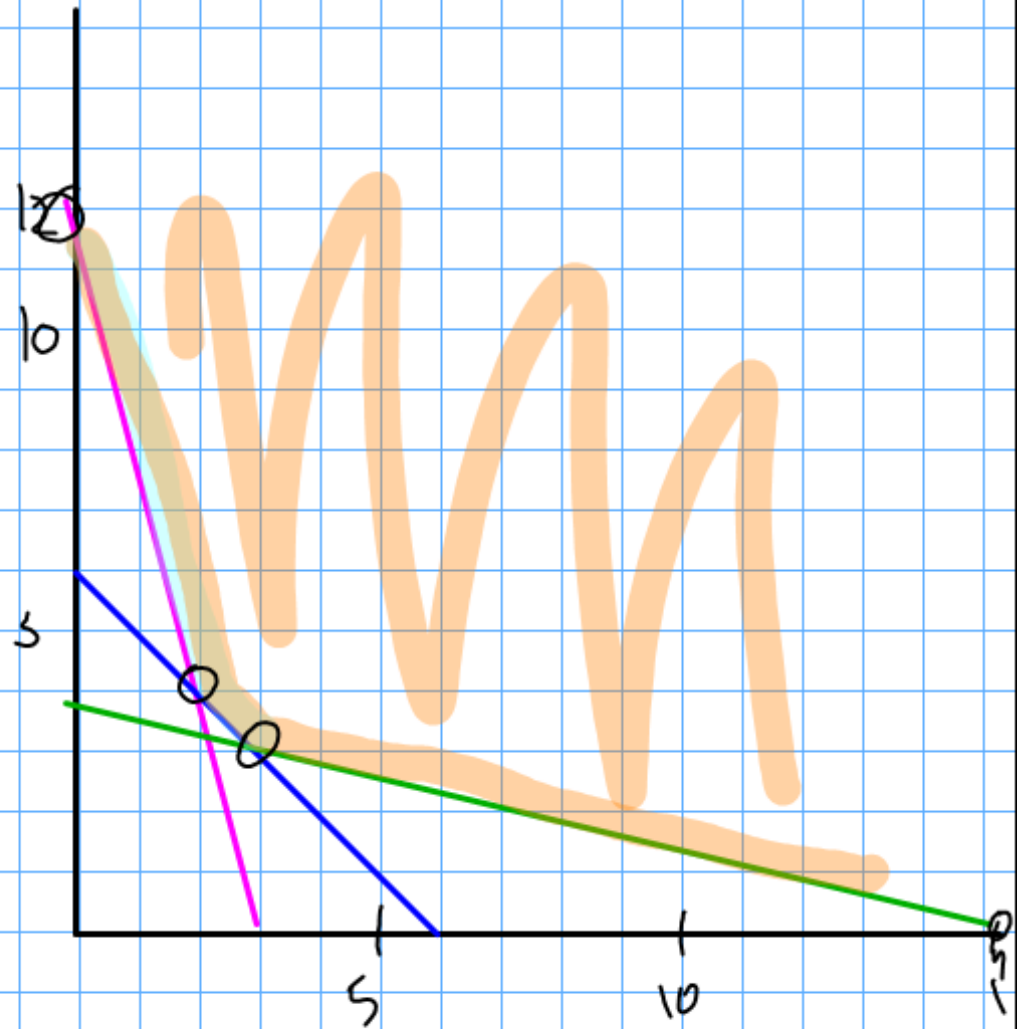
min. cost

$$2000x + 4000y$$

$$(2, 4) \Rightarrow 2000(2) + 4000(4) = \$20,000$$

$$(3, 3) \Rightarrow 2000(3) + 4000(3) = 6000 + 12,000 = \$18,000$$

Both factories op. for 3 days
\$18,000



4) Shauna is concerned about her cat Kiwi's diet. She wants to give Kiwi a mixture of canned food and dry food. Each ounce of canned food has 2 grams of protein and 4 grams of fat and costs \$0.10 per ounce. Each ounce of dry food has 6 grams of protein and 2 grams of fat and costs \$0.06 per ounce. Kiwi needs at least 30 grams of protein and at least 16 grams of fat. Kiwi should not eat more than 12 ounces of food per day.

- Write equations to represent the constraints, using x for canned food and y for dry food.
- Graph the inequalities and make a clear sketch of the feasible region. Label all relevant points on your graph.
- How many ounces of each kind of food should Kiwi eat so that the cost is minimized? What is the cost of feeding Kiwi for a day?

$x = \text{canned}; y = \text{dry food}$

protein : $2x + 6y \geq 30$

fat : $4x + 2y \geq 16$

food : $x + y \leq 12$

minimized =
cost $.10x + .06y$

$$2x + 6y \geq 30 \quad \begin{array}{c} x\text{-int} \\ 15 \end{array} \quad \begin{array}{c} y\text{-int} \\ 5 \end{array}$$

$$4x + 2y \geq 16 \quad \begin{array}{c} x\text{-int} \\ 4 \end{array} \quad \begin{array}{c} y\text{-int} \\ 8 \end{array}$$

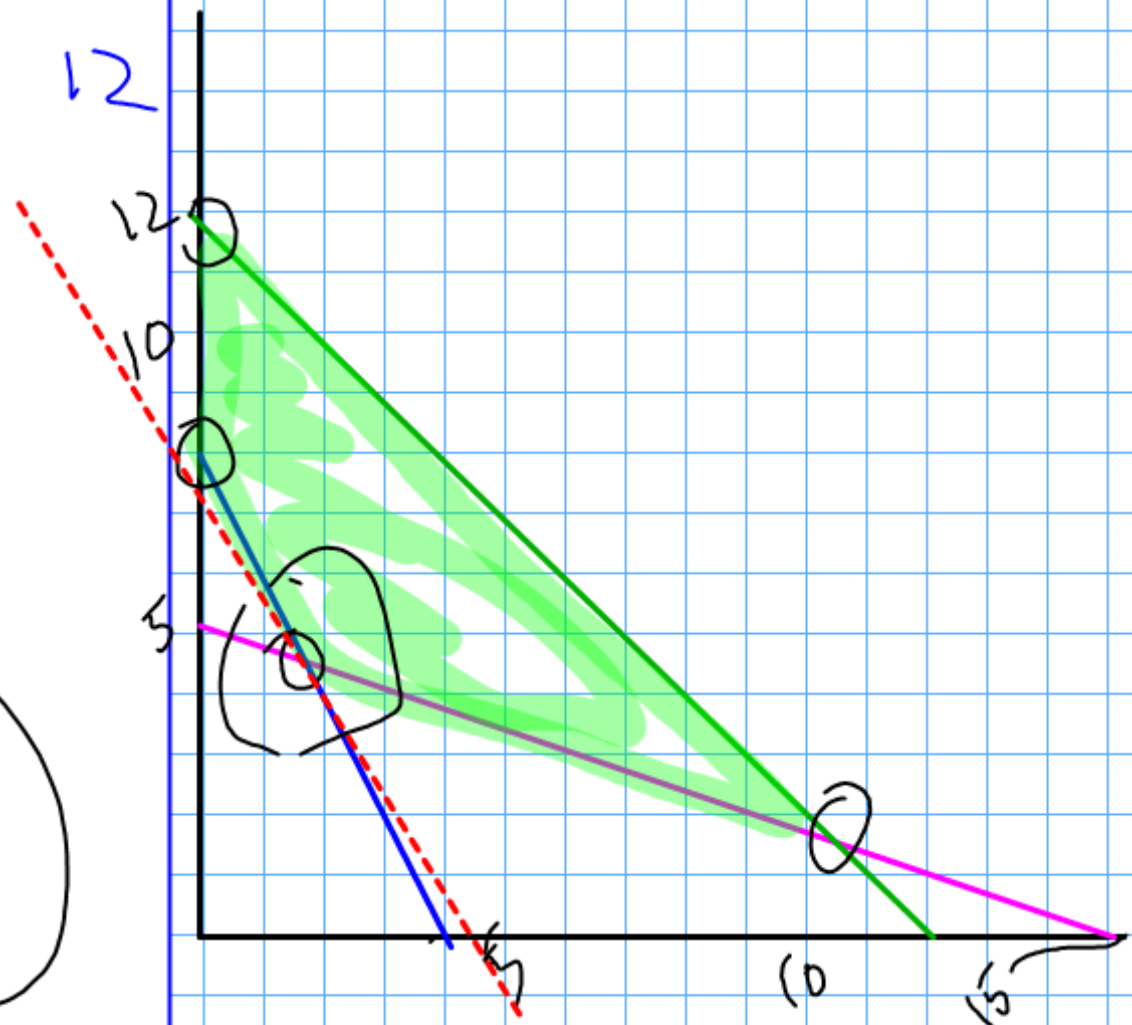
$$x + y \leq 12 \quad \begin{array}{c} x\text{-int} \\ 12 \end{array} \quad \begin{array}{c} y\text{-int} \\ 12 \end{array}$$

min. cost

$$.1x + .06y = .6$$

$$\begin{array}{c} x\text{-int} \\ 6 \end{array} \quad \begin{array}{c} y\text{-int} \\ 10 \end{array}$$

$$\begin{array}{l} x = 1.8 \\ y = 1.5 \\ 44\text{\$/day} \end{array}$$



Your group is to make up a linear programming problem. The key ingredients you need to have in your problem are:

- 1) Two Variables
- 2) A linear expression using those variables to be maximized or minimized
- 3) Three or Four constraints

Afterwards, solve it on a SEPERATE piece of paper.